



# Σύνθετα Δίκτυα

Διδάσκων –  
Δημήτριος Κατσαρός



# Εισαγωγή στα Σύνθετα Δίκτυα



# 2021 Nobel Prize in Physics



for groundbreaking contributions to our understanding of complex physical systems’,

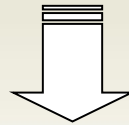
with half going to  
**Giorgio Parisi**

*‘for the discovery of the interplay of disorder and fluctuations in physical systems from atomic to planetary scales’*



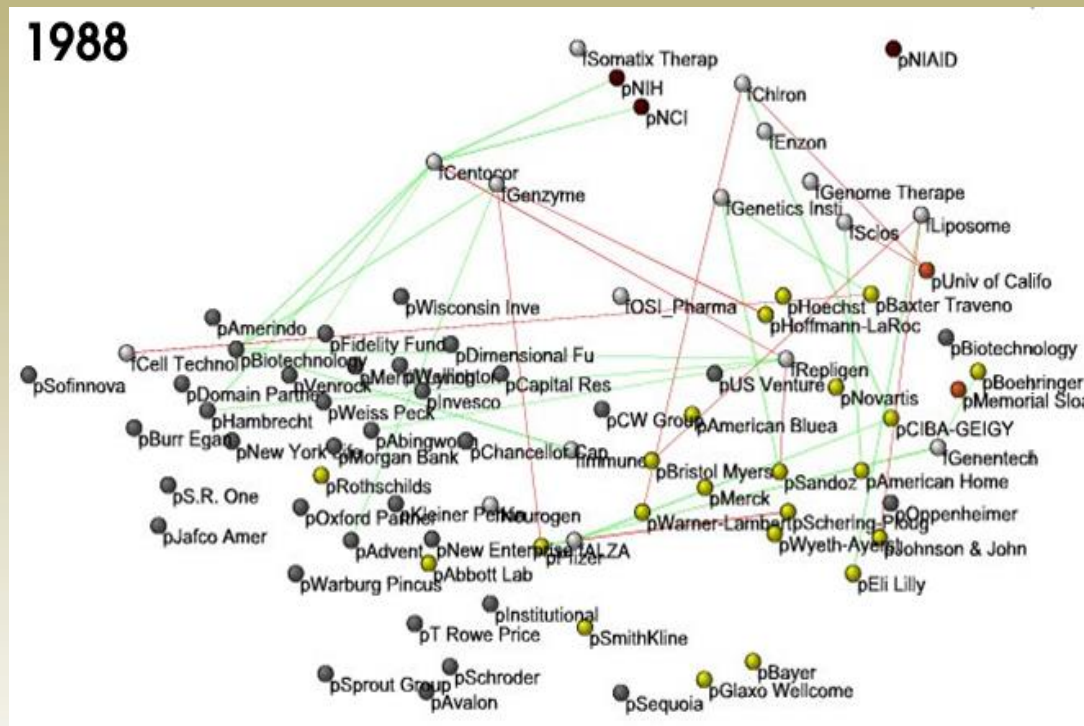
# Complex systems

Made of  
many non-identical **elements**  
connected by diverse **interactions**.



**NETWORK**

# Business ties in US biotech-industry



Nodes: companies: investment

pharma

research labs

public

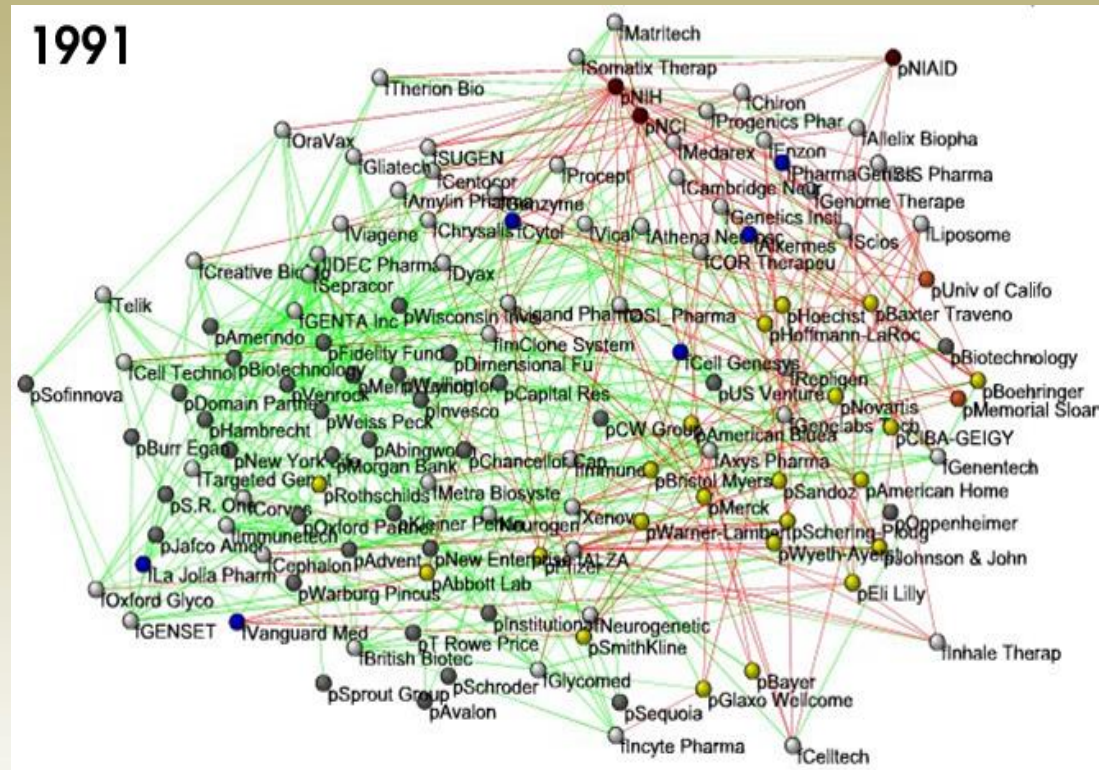
biotechnology

Links: financial

R&D collaborations



# Business ties in US biotech-industry



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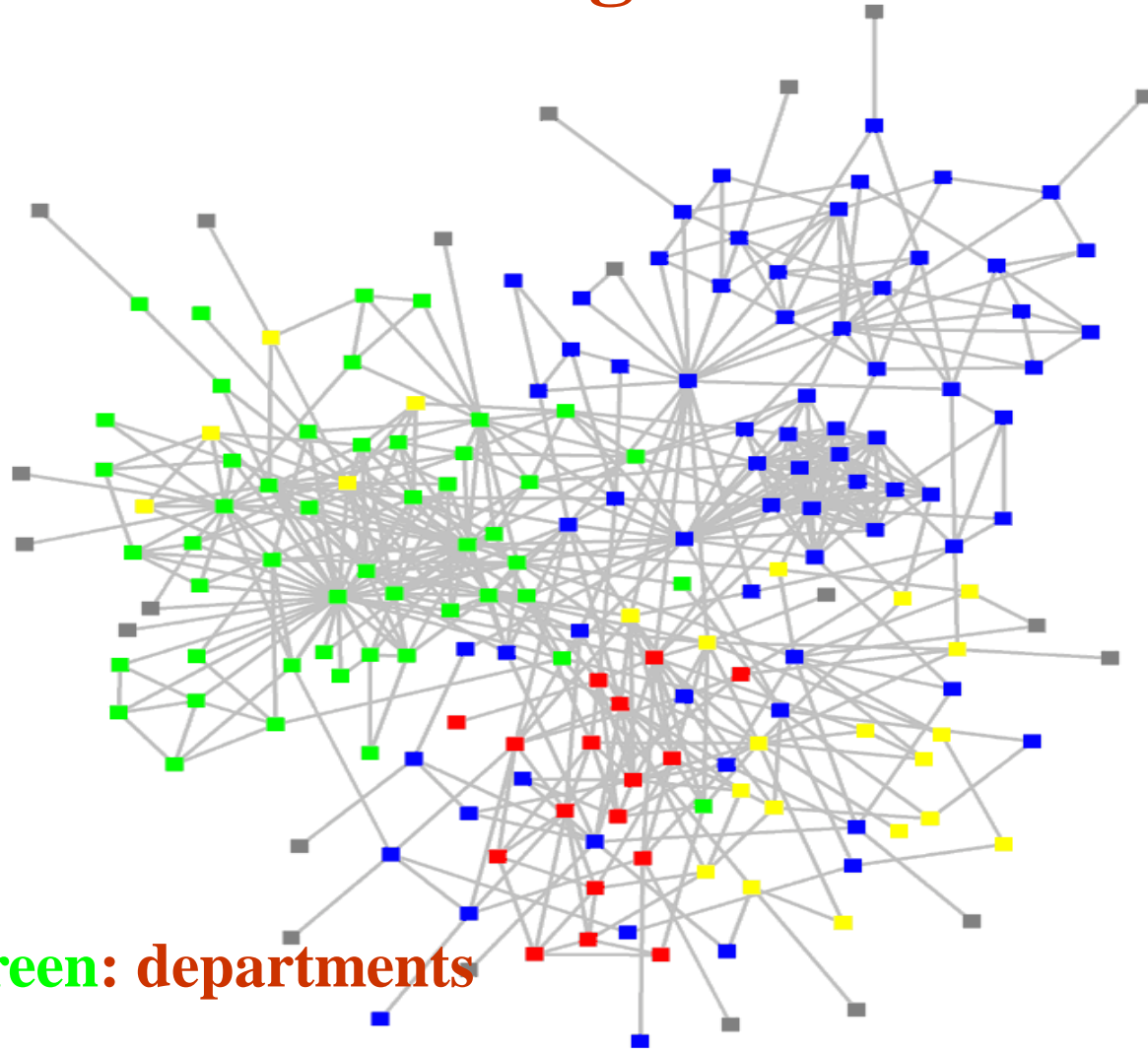
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# Structure of an organization

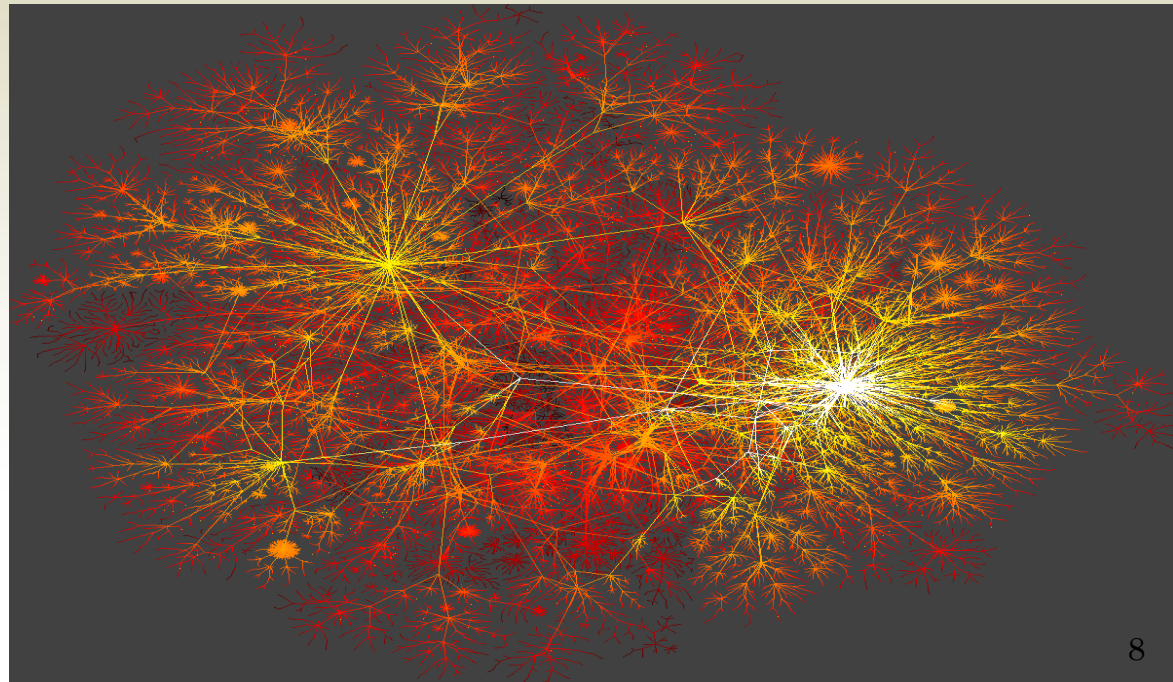
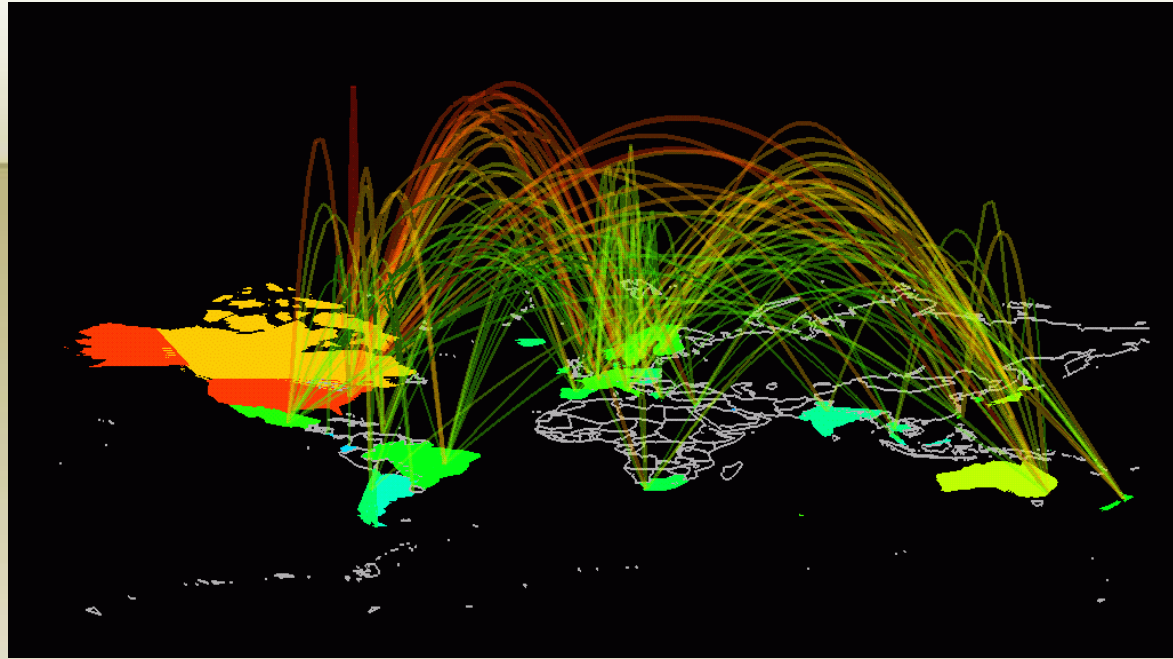


**Red, blue, or green: departments**

**Yellow: consultants**

**Grey: external experts**

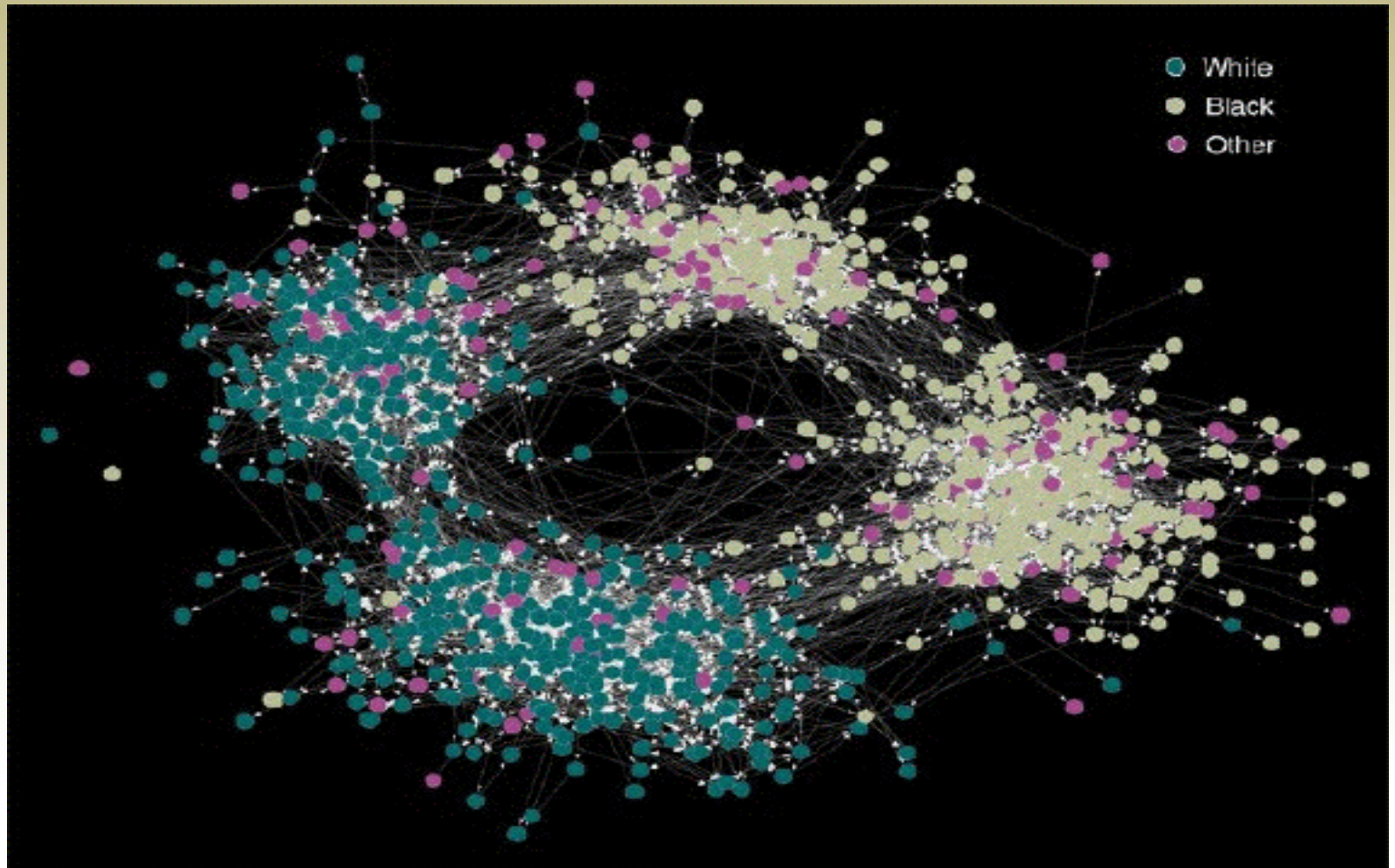
# Internet



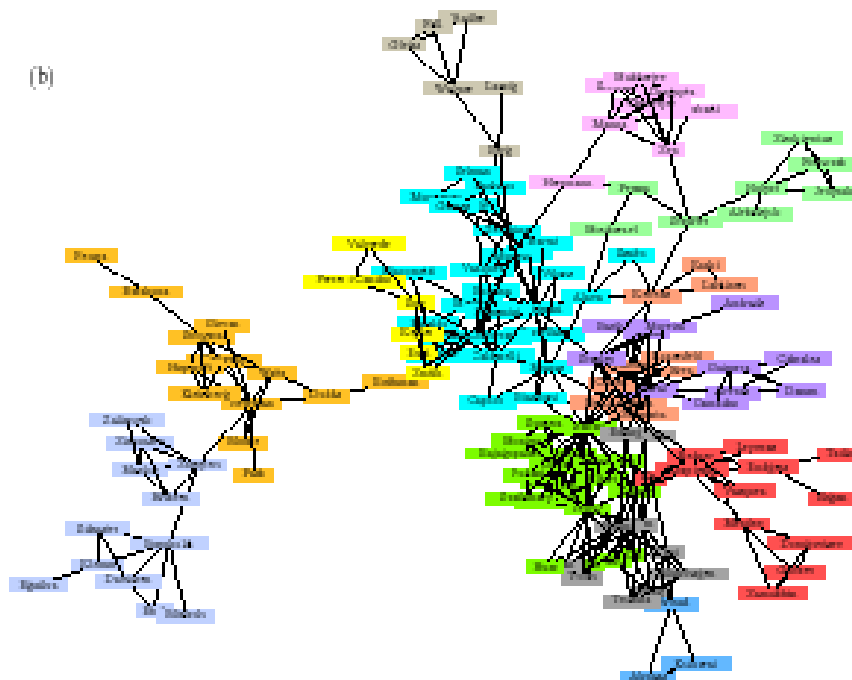
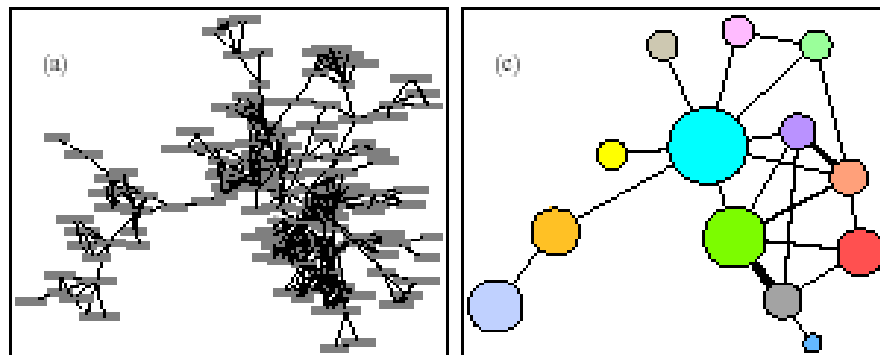




# Friendship Network



# Network Collaboration Network





## 9-11 Terrorist (?) Network

Social Network Analysis is a mathematical methodology for *connecting the dots* -- using science to fight terrorism.

Connecting multiple pairs of dots soon reveals an emergent *network* of organization.

# Swedish sex-web

**Nodes:** people (Females; Males)

**Links:** sexual relationships



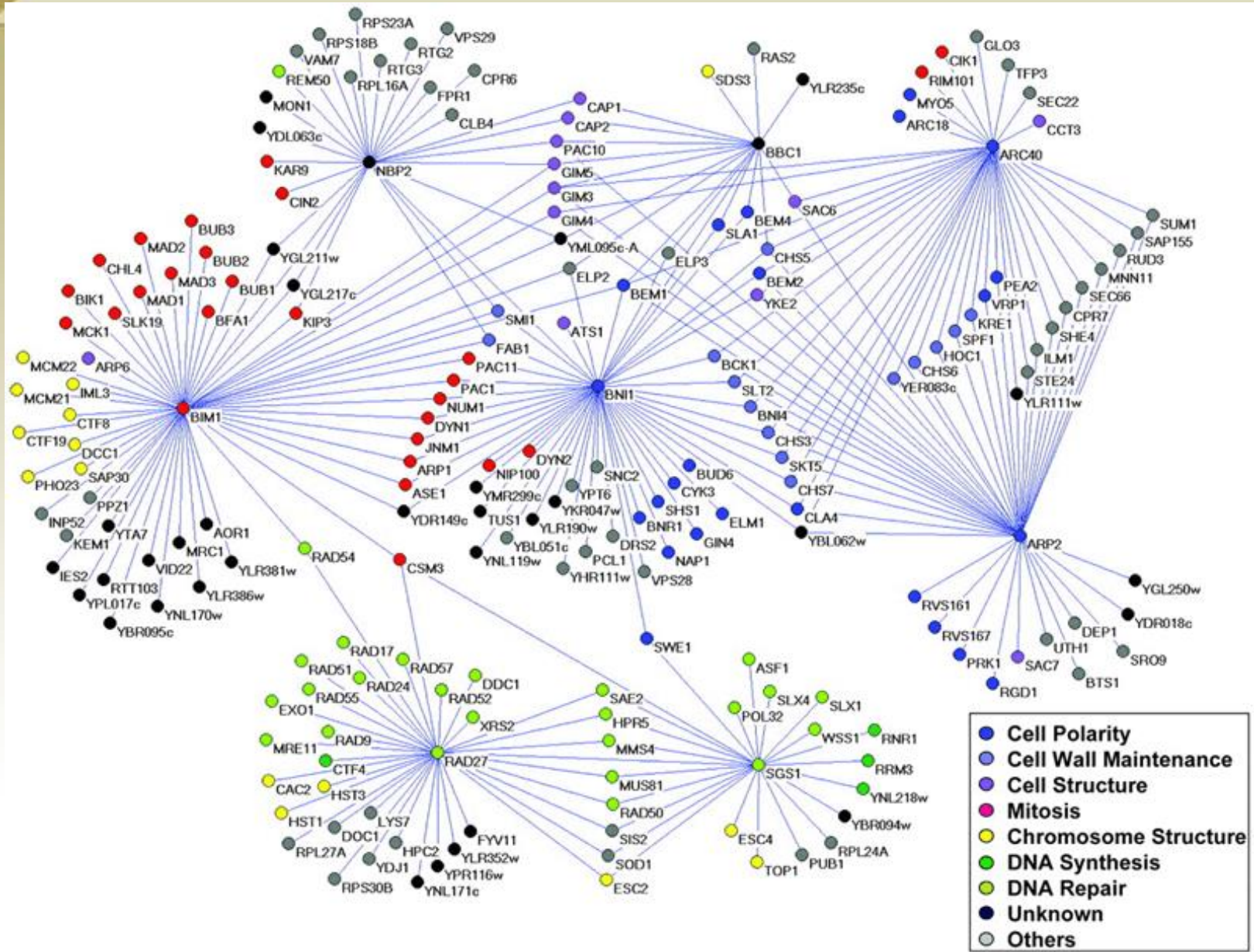
4781 Swedes; 18-74;  
59% response rate.

Liljeros et al. *Nature* 2001



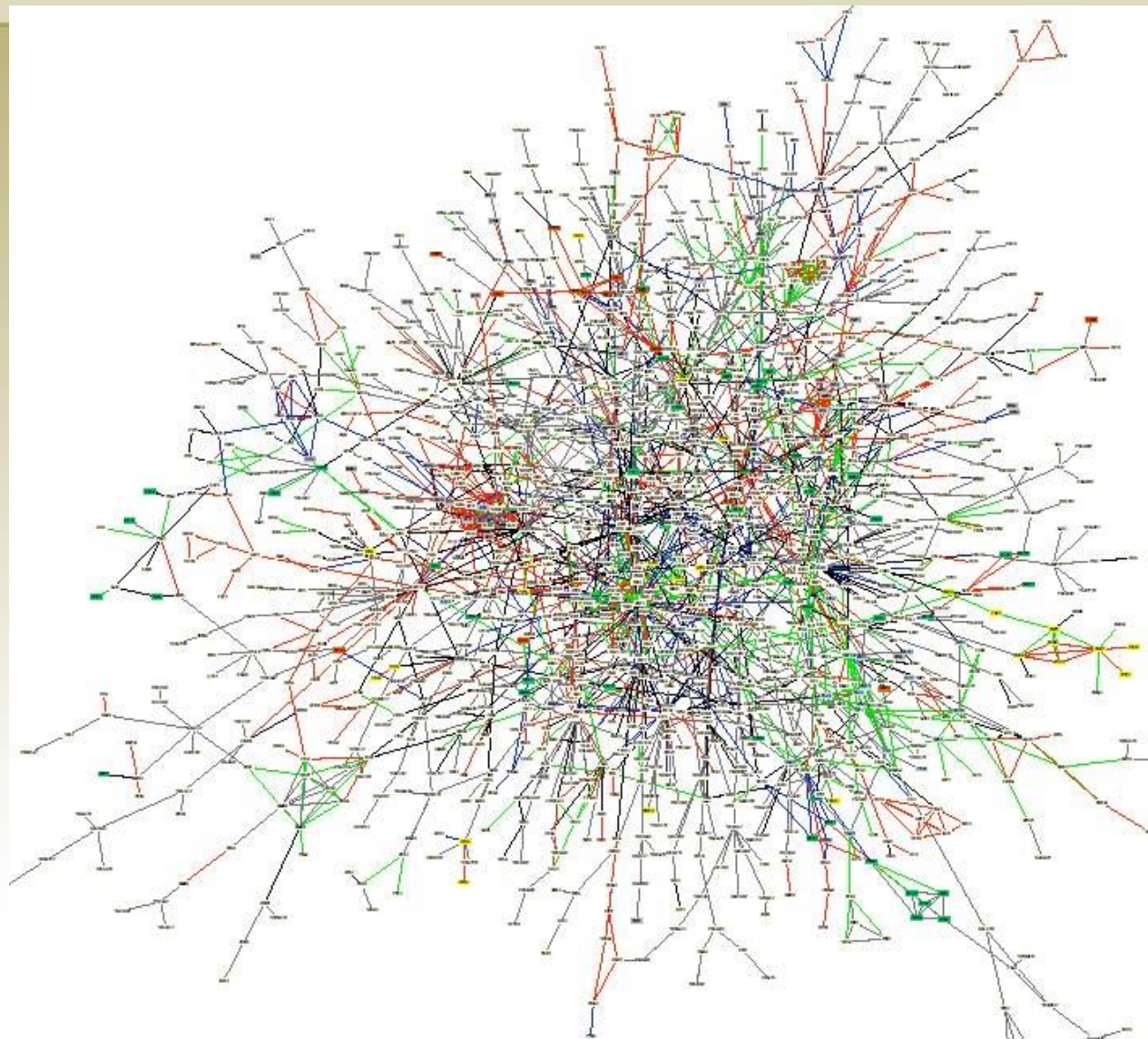


# Genetic interaction network





# Yeast protein-protein interaction network





## What Questions can be asked

- Does these networks display some symmetry
- Are these networks creation of intelligent objects or they have emerged.
- How have these networks emerged
  - Underlying simple rules leading to their complex formation





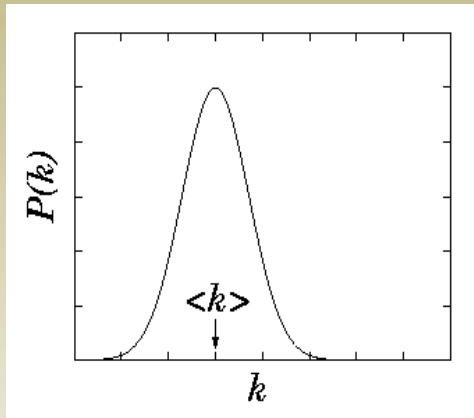
# What Questions can be asked

- Can we predict some outcomes/ make statements about the health of the system represented by the network
- Are these networks robust against failure
- Does these networks help in information flow
- How can we engineer (build) such network, (engineering complex systems).



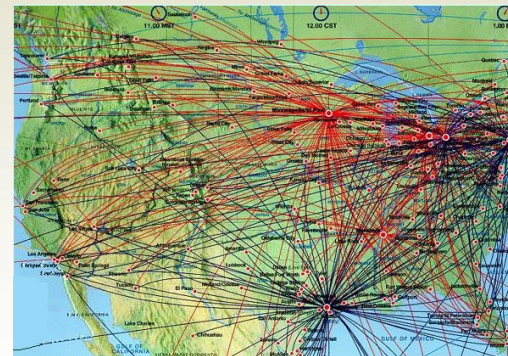
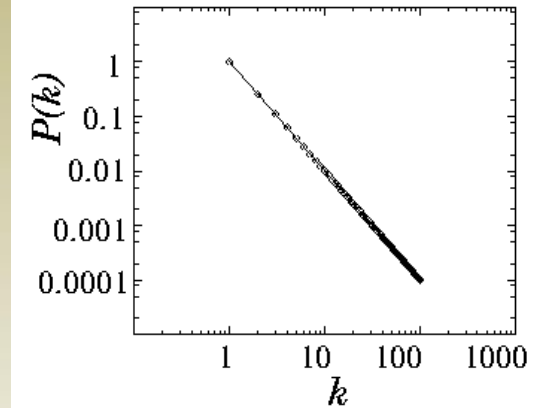
# Symmetry

Poisson distribution



**Exponential Network**

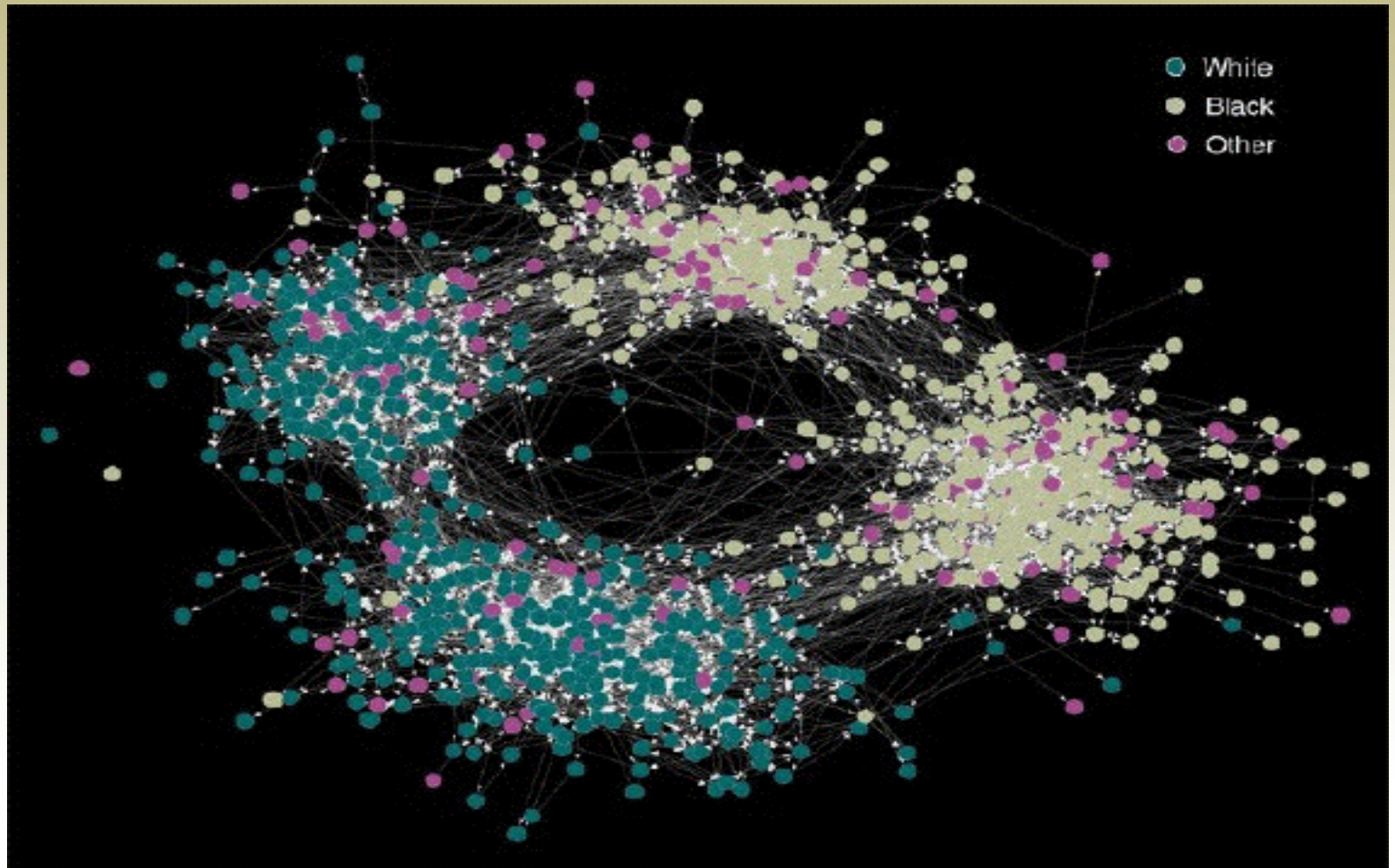
Power-law distribution



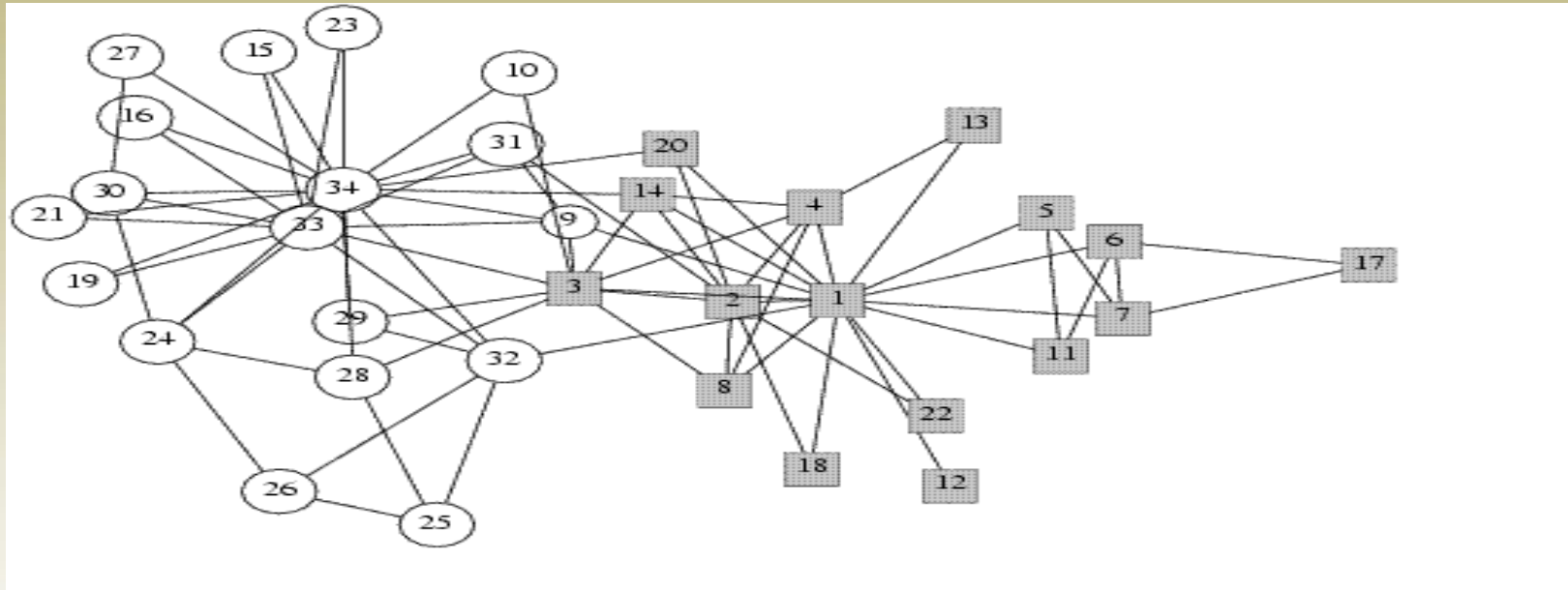
**Scale free Network**



# Friendship Network (Community)



# Karate Club



Instructors 1 and 33



# The Small World Effect

How do human contact patterns influence the spread of disease?



Outbreaks of SARS (Severe Acute Respiratory Syndrome)



# The Small World Effect

Even in very large social networks, the average distance between nodes is usually quite short.

Milgram's small world experiment:

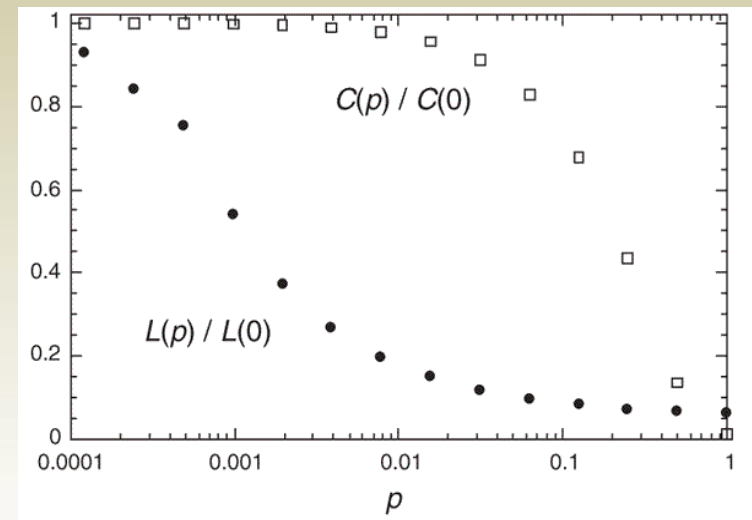
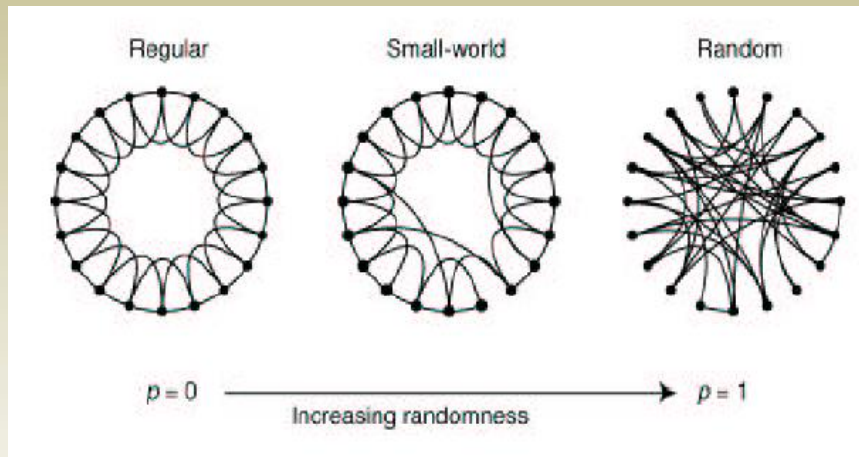
- Target individual in Boston
- Initial senders in Omaha, Nebraska
- Each sender was asked to forward a packet to a friend who was closer to the target
- Friends asked to do the same

**Result:** Average of 'six degrees' of separation.

S. Milgram, *The small world problem*, *Psych. Today*, 2 (1967), pp. 60-67.

# Watts-Strogatz ‘Small World’ Model (Simple Rules)

Watts and Strogatz introduced this simple model to show how networks can have both short path lengths and high clustering.



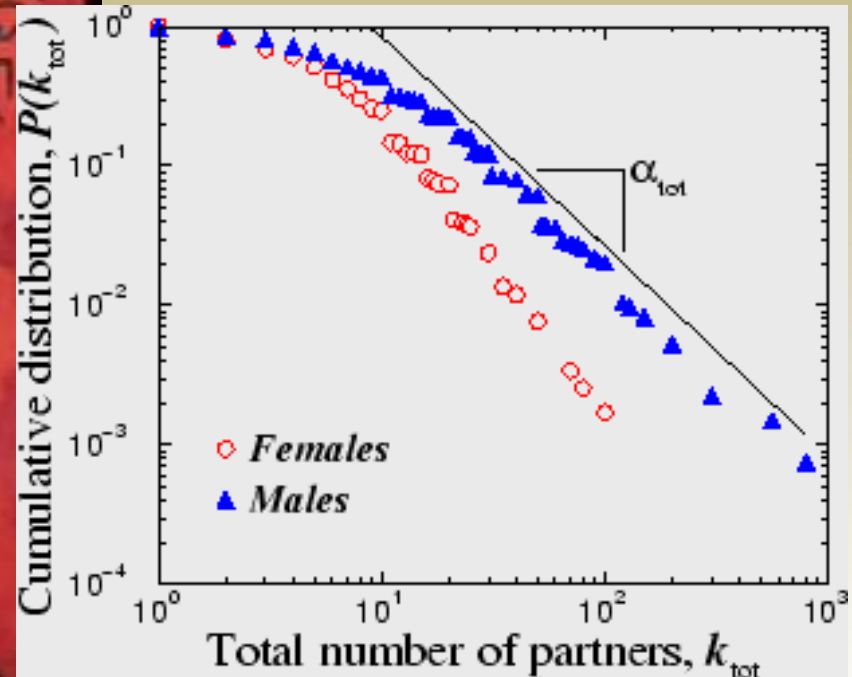
QuickTime™ and a  
TIFF (Uncompressed) decompressor  
are needed to see this picture.

D. J. Watts and S. H. Strogatz, *Collective dynamics of “small-world” networks*, *Nature*, 393 (1998), pp. 440–442.

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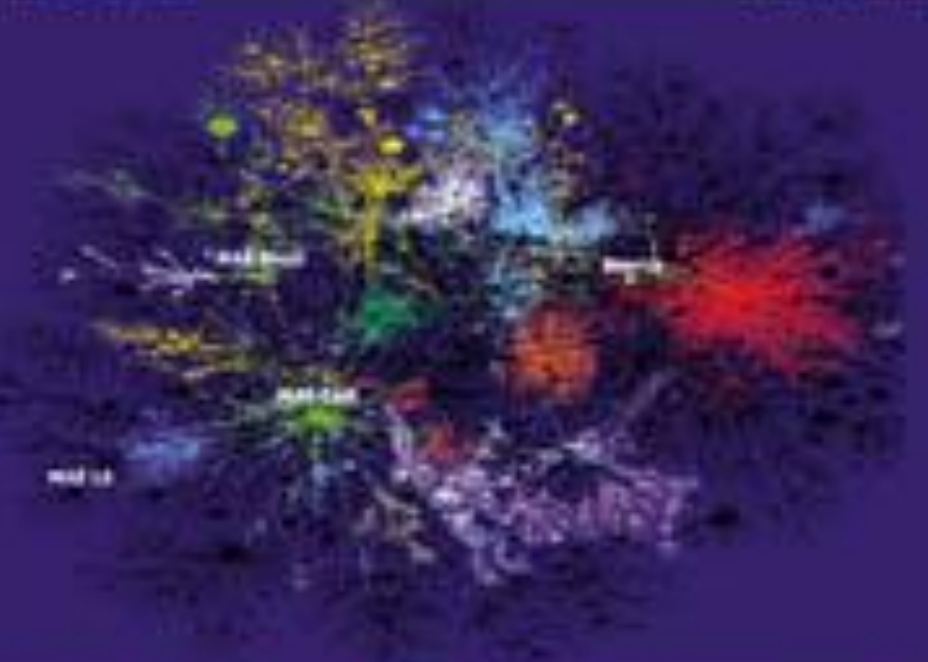




# Internet

- Robust against random failure
- Vulnerable against attack

27 July 2008 International weekly journal of science  
**nature**  
ISSN 0028-0836 www.nature.com



## Achilles' heel of the Internet

Obesity Mice that eat more but weigh less

Ocean anoxic events Not a flat sea

Cell signalling Fringe overcomes Notch

new on the market  
Opportunities



## 9-11 Terrorist (?) Network

### How to conduct investigation



## Some interesting Problems

- Consonants (Language) Networks
- Marriage Networks
- Collaboration Networks
- Build Networks which are robust as well as efficient
- Actors Network



# Course Outline

- Techniques to analyze networks
- Special types of networks – random networks, power law networks, small world networks
- Models of network growth
- Processes taking place on network – search, epidemics
- Centralities, communities, influentials

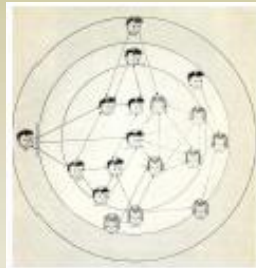


# Traditional vs. Complex Systems Approaches to Networks

## Traditional Questions:

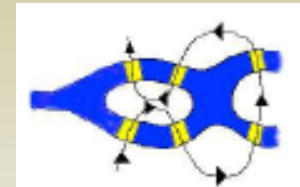
*Social Networks:*

Who is the most important person in the network?



*Graph Theory:*

Does there exist a cycle through the network that uses each edge exactly once?



## Complex Systems Questions:

What fraction of edges have to be removed to disconnect the graph?

What kinds of structures emerge from simple growth rules?

